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Erlangen

Skin Model Shapes: A new Paradigm for the Tolerance Analysis and the Geometrical Variations Modelling in Mechanical Engineering

Lehrstuhl für

Konstruktionstechnik

Friedrich-Alexander-Universität Erlangen-Nürnberg
Prof. Dr.-Ing. Sandro Wartzack



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and the Geometrical Variations Modelling
in Mechanical Engineering

Skin Model Shapes: Ein neues Paradigma für die Toleranzanalyse
und die Modellierung geometrischer Abweichungen im Maschinenbau

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Die vorliegende Arbeit wendet sich an Ingenieure und Wissenschaftler aus dem Bereich der virtuellen Produktentwicklung und angrenzender Disziplinen mit Schwerpunkt auf dem Toleranzmanagement. Sie stellt ein umfassendes Rahmenwerk für die Toleranzsimulation unter Berücksichtigung von Formabweichungen in Übereinstimmung mit internationalen Normen zur Geometrischen Produktspezifikation vor. Hierzu werden Algorithmen für die Erzeugung abweichungsbehafteter Punktwolken und Oberflächennetze (Skin Model Shapes), für deren Skalierung sowie deren Montage-simulation erarbeitet. Darüber hinaus behandelt die Arbeit die Toleranzanalyse bewegter Mechanismen und stellt einen Software-Prototypen für die Toleranzsimulation mittels Oberflächennetzen vor. Auf Basis der kritischen Gegenüberstellung von Ergebnissen des erarbeiteten Verfahrens mit bestehenden Toleranzanalysemethoden für typische Problemfälle wird gezeigt, dass durch die Berücksichtigung von Formabweichungen bei der Toleranzanalyse die Einflüsse von Bauteilabweichungen auf die Funktion und Qualität mechanischer Baugruppen und bewegter Systeme deutlich realitätsnäher bestimmt und dadurch Toleranzentscheidungen optimiert werden können.

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Preface

The current work was developed during my time as an academic counsellor at the Institute of Engineering Design KTMfk of the FAU Erlangen-Nürnberg. During that time, I received great support from and I was influenced by many persons, to whom I am sincerely grateful.

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March 2017

Benjamin Schleich

– *Meinen Eltern* –

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Abbreviations and Symbols

Abbreviations

ANOVA	Analysis of Variance
ASME	American Society of Mechanical Engineers
BC	Before Christ
BRep	Boundary Representation
CAD	Computer-Aided Design
CAM	Computer-Aided Manufacturing
CAPP	Computer-Aided Process Planning
CAT	Computer-Aided Tolerancing
CLTE	Closed-Loop Tolerance Engineering
CMM	Coordinate Measuring Machine
CSG	Constructive Solid Geometry
CZ	Common Zone
D	Dimension
DIN	Deutsches Institut für Normung (German Institute for Standardization)
DLM	Direct Linearisation Method
DoF	Degree of Freedom
E. g.	Exempli Gratia
(E)FAST	(Extended) Fourier Amplitude Sensitivity Test
FEA	Finite Element Analysis
GD&T	Geometric Dimensioning and Tolerancing
GPS	Geometrical Product Specification
GUI	Graphical User Interface
I. a.	Inter alia
I. e.	Id est
I. i. d.	Independent and Identically Distributed
ICDF	Inverse Cumulative Distribution Function
ICP	Iterative Closest Point
IGES	Initial Graphics Exchange Specification
ISO	International Organization for Standardization
ITP	Integrated Tolerancing Process
KC	Key Characteristic
KDE	Kernel Density Estimate
LHS	Latin Hypercube Sampling
LSC	Least-Squares Circle/Cylinder
LSL	Lower Specification Limit
MBD	Model-based Definition
MCC	Minimum Circumscribed Circle/Cylinder
MIC	Maximum Inscribed Circle/Cylinder

MZC	Minimum Zone Circle/Cylinder
NC	Numerically Controlled
NURB	Non-Uniform Rational B-Spline
(K)PCA	(Kernel) Principal Component Analysis
PCFR	Place, Clamp, Fasten, and Release
PDF	Probability Density Function
PDM	Point Distribution Model
PMI	Product and Manufacturing Information
RD(M)	Robust Design (Methodology)
SDT	Small Displacement Torsor
SMS	Skin Model Shapes
SPC	Statistical Process Control
SSA	Statistical Shape Analysis
STEP	Standard for the Exchange of Product Model Data
STL	STereoLithography File Format
TC	Technical Committee
TCA	Tooth Contact Analysis
TTRS	Technologically and Topologically Related Surfaces
USL	Upper Specification Limit
VDA	Verband der Automobilindustrie (German Assoc. of the Automotive Industry)
VDI	Verein Deutscher Ingenieure (Association of German Engineers)
WC	Worst-Case
WP	Workpiece

Symbols

a, b, m, k, K	Cost-Function Parameters
\mathbf{b}	Scores, Axis Direction
$\tilde{\mathbf{b}}$	Random Scores
c	Cost (Tolerance-related)
c_a	Process Accuracy Index
c_p	Process Precision Index
c_{pk}	Process Capability Index
c_{pm}	“Taguchi” Index
d	Dimension, Distance
d'	Radial Distance
d_{PS}	Projected (signed) Distance
d_{PSN}	Normal Distance
f	Tolerance Analysis Function, Probability Density, Facet of the Convex Hull
\mathbf{f}	Stochastic Process with Approximation \mathbf{f}
h	Systematic Deviations (Point-wise), Height
l_ρ	Correlation Length
m	Module
n	(Vertex) Normal Vector

p	Point $\in \mathbb{R}^3$
\mathbf{r}	Rotations
t	Tolerance, Point in Time, Translations
\mathbf{w}	Assembly Direction
x	Point $\in \mathbb{R}^3$
\hat{x}	Center of a Skin Model Shape
\hat{x}^f	Center of a Skin Model Shape Feature
\tilde{x}	Point $x \in \mathbb{R}^3$ with systematic Deviations
\bar{x}	Point $x \in \mathbb{R}^3$ with systematic and random Deviations
\underline{x}	Footpoint
C	Total Cost (Tolerance-related), Covariance Function
\mathbf{C}	Correlation Matrix
CV	Convex Hull Volume
F	Force Slope of the Assembly Force
F_r	Runout Error
K	Cost Coefficient (Quality Loss)
L	Quality-Loss
P	Precision Factor
\mathbf{P}	Force Application Point of the Assembly Force
R^2	Coefficient of Determination
S	Difference Surface
\mathbf{X}	Skin Model Shape as a Set of Points in \mathbb{R}^3
\mathbf{X}^f	Skin Model Shape Feature ($\mathbf{X}^f \subset \mathbf{X}$)
$\bar{\mathbf{X}}$	Mean (Skin Model) Shape
$\tilde{\mathbf{X}}$	Approximation of \mathbf{X}
Y	Key Characteristic
α	Rotation Angle
$\boldsymbol{\alpha}$	Rigid Body Transformation
α^E	Transmission Error
β	Regression Coefficients
$\boldsymbol{\beta}$	Parameter Vector
δ	Moment-independent Sensitivity Measure
ζ	Euclidean Distance
μ	Expectation, Sample Mean
ξ	Linearity Coefficient
$\boldsymbol{\xi}$	Gaussian Random Variables (i. i. d.)
ρ	Correlation Function
σ	Standard Deviation, Sample Standard Deviation
$\boldsymbol{\tau}$	Small Displacement Torsor
\mathbf{X}	Random Variables (Spatially correlated)

ψ	Standard Gaussian Random Variables (i. i. d.)
ω	Weights
ω	Rotations (Small Displacement Torsor) with $\alpha \equiv r_x, \beta \equiv r_y, \gamma \equiv r_z$
Δp	Displacement of p
Δt	Time Discretization
Φ	Main Modes of Variation

Indices

i, n	1, 2, 3, ...	Counting Indices
ψ	1, 2, 3, ...	Assembly Steps

Zusammenfassung

In Zeiten scharfen internationalen Wettbewerbs steigt der Druck auf Unternehmen qualitativ hochwertige Produkte mit moderaten Fertigungskosten anzubieten. Obgleich moderne Fertigungsverfahren stetig steigende Fertigungsgenauigkeiten erreichen, sind dennoch die Produktqualität und die Montierbarkeit als wesentlicher Treiber für die Fertigungskosten durch geometrische Bauteilabweichungen beeinflusst, die zwangsläufig an jedem gefertigten Bauteil zu beobachten sind. Daher existiert eine dringende Notwendigkeit für Unternehmen, diese Abweichungen und deren Auswirkungen entlang des Produktlebenszyklus zu steuern. Um dies innerhalb der Zeit- und Kostenbudgets umzusetzen, werden Produkt- und Prozessentwickler durch Toleranzsimulationsprogramme unterstützt, die die frühzeitige Vorhersage der Auswirkungen von geometrischen Bauteilabweichungen auf Produkteigenschaften ohne zeit- und kostenintensive physikalische Prototypen erlauben. Allerdings bringen bekannte Methoden und Werkzeuge zur Toleranzanalyse und deren zugrundeliegende mathematische Ansätze zur Abbildung geometrischer Abweichungen, Spezifikationen und Anforderungen schwerwiegende Nachteile in Hinblick auf die Berücksichtigung von Formabweichungen mit sich und sind nicht vollständig konform zu internationalen Tolerierungsnormen.

Als Antwort auf diese Nachteile wurde das Konzept der Skin Model Shapes als neues Paradigma für die Modellierung von Produktgeometrie unter Berücksichtigung geometrischer Abweichungen entwickelt. Es nutzt punktbasierete Modelle zur Abbildung der Produktgeometrie in Anbetracht aller Arten geometrischer Abweichungen. Die vorliegende Arbeit untersucht die Grundlagen des Konzepts der Skin Model Shapes, demonstriert seine Potentiale für die Abbildung von abweichungsbehafteter Produktgeometrie entlang des Produktlebenszyklus und zeigt wesentliche Anwendungsfelder dieses Konzepts im Kontext des Toleranzmanagements auf. Zudem wird ein Toleranzanalyseansatz auf Basis von Skin Model Shapes vorgestellt, der verschiedene Algorithmen für die Erzeugung und Verarbeitung von Bauteilrepräsentanten in diskreter Geometrie nutzt und die realistische Vorhersage der Auswirkungen von geometrischen Bauteilabweichungen auf funktions- und qualitätskritische Schließmaße erlaubt. Die vorgestellten Ergebnisse dieses Ansatzes zur Toleranzanalyse für verschiedene Problemfälle belegen, dass Formabweichungen deutlichen Einfluss auf verschiedene Produkteigenschaften haben und dass das Konzept der Skin Model Shapes sowie der vorgestellte Toleranzanalyseansatz ein theoretisch fundiertes Rahmenwerk bilden, das die Nachteile bekannter Toleranzanalyseverfahren überwindet.

Abstract

In times of fierce international competition, the need for companies increases to deliver high-quality products manufactured at moderate costs. However, even though modern manufacturing processes offer steadily increasing accuracy, the product quality as well as the product assemblability as a main driver for the manufacturing costs are influenced by geometrical part deviations, which are inevitably observed on every manufactured workpiece. Thus, there exists a strong need for companies to manage these deviations and their effects throughout the whole product life-cycle. In order to perform this within time and cost constraints, computer-aided tolerancing tools support product and process development teams by enabling the early prediction of the effects of geometrical part deviations on product characteristics without the need for cost and time expensive physical mock-ups. However, established tools for the tolerance analysis and their underlying mathematical approaches for the representation of geometrical deviations, geometrical specifications, and geometrical requirements imply severe shortcomings regarding the consideration of form deviations and lack of a full conformance to international tolerancing standards.

As a response to these shortcomings, the concept of Skin Model Shapes has been developed as a new paradigm for the modelling of product geometry considering shape variability. It employs point-based models for the representation of part geometry considering all different kinds of geometrical deviations. The present work explores the fundamentals of the concept of Skin Model Shapes, demonstrates its potentials for the representation of product geometry considering geometrical variations along the product life-cycle, and illustrates main applications of this concept in the context of geometrical variations management. Moreover, a tolerance analysis approach utilising the concept of Skin Model Shapes is proposed, which employs various algorithms for the generation and processing of discrete geometry Skin Model Shapes and which allows the realistic prediction of the effects of geometrical variations and tolerance specifications on product key characteristics. The results obtained by this novel tolerance analysis approach for various study cases highlight, that form deviations have distinct effects on geometrical product characteristics and that the concept of Skin Model Shapes and the tolerance analysis based thereon offer a sound theoretical framework and theory, which overcomes severe shortcomings of established tolerance analysis approaches.

